

End Semester/Reappear (Semester II) Examination July 2022

Programme: ABM Subject: Operation Research Subject Code: 11.558 Enrollment No:

Section I

1. Short Answer type questions. Answer any four.

- a. Define slack and surplus. Explain the purpose of these variables.
- b. Brief about the three methods by which transportation problems can be solved.
- c. Define (i) Pure Strategy, (ii) Mixed Strategy, (iii) Saddle Point, (iv) Zero sum game
- d. Describe game theory problems in brief.
- e. Explain Economic Order Quantity (EOQ) model with static demand.
- f. Explain Project Evaluation and Review Technique (PERT).

Section II

Long Answer type questions. Answer any three.

2. A company is in the process of preparing a budget for launching a new product. The following table provides the associated activities and their duration.

| Name of activity | Description of activity | Predecessor(s) | Duration (days) |
|------------------|-----------------------------|----------------|------------------------|
| А | Forecast sales volume | | 10 |
| В | Study comparative market | | 7 |
| С | Design items and facilities | A | 5 |
| D | Prepare production schedule | С | 3 |
| Е | Estimate cost of production | D | 2 |
| F | Set sales price | B,E | 1 |
| G | Prepare budget | E,F | 14 |

Prepare a project network diagram.

3. There are four warehouses and three market places from where demands are received. The warehouse capacities and market demands are for a given month are given. The transportation costs (in rupees) per unit from warehouses to demand canters are also given below.

| | D1 | D2 | D3 | D4 | Warehouse Capacity |
|---------------|-----|-----|-----|-----|--------------------|
| W1 | 11 | 13 | 17 | 14 | 250 |
| W2 | 16 | 18 | 14 | 10 | 300 |
| W3 | 21 | 24 | 13 | 10 | 400 |
| Total Demands | 200 | 225 | 275 | 250 | |

Using above data, find minimum transportation cost using North-West method. Write the optimal allocation of number of units transported.

4. Table below shows pay-off matrix with respect to player A. Reduce pay off matrix using dominance property and find saddle point, value of the game, probability of optimum strategy of the players.

| | Player B, Strategy1 | Player B, Strategy2 | Player B, Strategy3 | Player B, Strategy4 | Player B, Strategy5 |
|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|
| Player A, Strategy1 | 54 | 28 | 29 | 30 | 37 |
| Player A, Strategy2 | 37 | 16 | 25 | 28 | 33 |
| Player A, Strategy3 | 78 | 39 | 51 | 40 | 46 |
| Player A, Strategy4 | 11 | 12 | 48 | 23 | 27 |

5. Discuss Scope and Applications of Operation Research in managerial decision making.

Full Marks: 70 Time: 3 Hrs.

 $4 \ge 5 = 20$

 $3 \ge 10 = 30$

6. Use Big M method to solve

$Max Z = 2x1 + x2 + 3x3, \quad x1 + x2 + 2x3 \le 5, \qquad 2x1 + 3x2 + 4x3 = 12, \ x1, x2, x3 \ge 0$

Section III

 $1 \ge 20 = 20$

Application based questions. Answer any one.

7. Data of ABC Auto Ltd., a car manufacturing company are given below. Distance (in km.) chart between Plants and Distribution centers of ABC Auto Ltd.

| | Distribution center-1 | Distribution center-2 |
|---------|-----------------------|-----------------------|
| Plant-1 | 1400 | 4300 |
| Plant-2 | 1600 | 1850 |
| Plant-3 | 1650 | 1100 |

Cost of transportation per car per km. is Rs. 8

Chart for total production per plant and total demand per distribution center.

| | Distribution center-1 | Distribution center-2 | Total production |
|-----------------|-----------------------|-----------------------|------------------|
| Plant-1 | | | 800 |
| Plant-2 | | | 1200 |
| Plant-3 | | | 1000 |
| Total Demand => | 1900 | 1100 | |

Questions:

- a. Write the "transportation cost table" (transportation cost of one car from a plant to a distribution center. (4 marks).
- b. Write all linear equations and constraints related to above problem. (4 marks)
- c. Write linear equation for total cost of transportation of all cars from Plants to Distribution Centers. (1 mark)
- d. Find optimal solution (values of x_{ij}) for minimum total cost of transportation. (7 marks)
- e. Calculate minimum total cost of transportation. (4 marks)
- 8. Table below shows pay-off matrix with respect to player A. Find value of the game, probability of optimum strategy of the players.

| | Player B, Strategy1 | Player B, Strategy2 | Player B, Strategy3 | Player B, Strategy4 |
|---------------------|------------------------|---------------------|---------------------|---------------------|
| Player A, Strategy1 | 2 | 2 | 3 | -1 |
| Player A, Strategy2 | 4 | 3 | 2 | 6 |

9. A publisher has a contract with an author to publish a book. The associated activities are given below. The author is required to submit hard copy and a soft copy of the manuscript. Prepare a project network diagram. Evaluate the earliest start time and latest completion time at each node of the network. Find the critical path and duration to complete the project.

| Name of activity | Description of activity | Predecessor(s) | Duration (Weeks) |
|------------------|--|----------------|------------------|
| A | Manuscript proofreading by editor | | 3 |
| В | Sample pages preparation | | 2 |
| C | Book cover design | | 4 |
| D | Artwork preparation | | 3 |
| Е | Author's approval of manuscript and sample | A,B | 2 |
| | pages | | |
| F | Book formatting | E | 4 |
| G | Author's review of formatted pages | F | 2 |
| Н | Author's review of artwork | D | 1 |
| Ι | Production of printing plates | G,H | 2 |
| J | Book production and binding | C,I | 4 |